Solving One-Step Equations

Objectives:

...to solve one-step equations involving whole numbers

Assessment Anchor:

7.D.2.1 – Select and/or use appropriate strategies to solve or represent number sentences.

Yocabulary alert!!

EQUATION – a mathematical sentence that uses an equals (=) sign to indicate that the side to the left of the equals sign has the same value as the side to the right of the equals sign

<u>INVERSE OPERATIONS</u> – operations that undo each other

NOTES

***EQUATIONS ARE LIKE BALANCED SEE-SAWS...AND <u>MUST REMAIN</u> BALANCED!!

To solve a one-step equation:

- 1. Locate the variable in the equation
- 2. Use the inverse (opposite) operation on both sides of the equation
- 3. Show your answer



"For every equation from this day forward, I agree to write down what I'm doing to both sides!"

Solving One-Step Equations

EXAMPLES

1)
$$x - 7 = 15$$

.....original problem

$$x - 7 = 15 + 7 + 7$$

.....locate the variable termadd 7 to both sides

$$x = 22$$

.....show final answer!

$$2) x + 10 = 57$$

.....original problem

$$\begin{array}{c} x + 10 = 57 \\ -10 - 10 \end{array}$$

.....locate the variable termsubtract 10 from both sides

$$x = 47$$

.....show final answer!

3)
$$8y = 72$$

.....original problem

$$8y = 72$$

.....locate the variable termdivide by 8 on both sides

$$y = 9$$

.....show final answer!

4)
$$13 = \frac{k}{4}$$

.....original problem

$$4 \times 13 = \frac{k}{4} \times 4$$

.....locate the variable term, and then multiply both sides by 4

$$\boxed{52 = k}$$

.....show final answer!

Solving One-Step Equations

5)
$$x + 13 = 19$$

9)
$$46 = y - 20$$

6)
$$x - 10 = 22$$

10)
$$41 = k + 18$$

7)
$$\frac{w}{7} = 14$$

11)
$$3k = 126$$

8)
$$135 = 5m$$

12)
$$22 = \frac{f}{6}$$



"Knowing to use inverse operations, and to write it down on both sides...that's our main goal here. It's just as important as calculating the right answer... maybe even MORE important."

One-Step Equations: Integers Mixed Operations Level 1: S1

Solve each equation.

1)
$$10 = z + 6$$

2)
$$8y = 48$$

3)
$$q - 12 = 1$$

4)
$$18 = \frac{a}{2}$$

5)
$$\frac{r}{3} = 7$$

6)
$$11 = m - 4$$

7)
$$t - 19 = 2$$

8)
$$1 + s = 3$$

10)
$$\frac{v}{5} = 9$$

Extra Practice

Find the opposite of each integer.

Find the opposite of the opposite of each integer.

Evaluate each expression.

- **36.** The balance of Bryce's account is \$16. Jada's account is \$5 overdrawn. What is the difference between their account balances?
- 37. A football team lost 3 yards on their first play and 6 yards on their second play. How many total yards did they lose?
- **38.** The table shows the lowest elevations for several states. Is the absolute value of the lowest elevation of California greater than or less than the absolute value of the lowest elevation of Illinois?

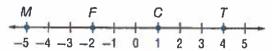
State	Lowest Elevation (ft)
Oklahoma	289
Illinois	279
Kentucky	257
California	-282





Test Practice

- **41.** If x = -1 and y = -2, then which of the following statements is true?
 - (A) |x| > 1
 - $^{\textcircled{B}}$ |x| < |y|
 - (C) |y| < 1
 - \bigcirc |y| < x
- 42. Refer to the number line below. Which point represents the number with the greatest absolute value?



- (F) point M
- (G) point F
- (H) point C
- ① point T

43. A video game has different point values associated with different actions. The table shows some of the actions. Which action has associated points with the greatest absolute value?

Action	Points
collect gem	+5
fall in water	-10
build bridge	+12
climb tree	-15

- (A) collect gem
- © build bridge
- (B) fall in water
- (D) climb tree
- 44. Which expression has the greatest value?
 - (F) |-25|
- . (H) |18|
- G |-16|
- 122
- 45. Short Response The table shows the freezing point of different liquids. What liquid's freezing point has the greatest absolute value?

Liquid	Freezing Point (°F)
Water	32
Acetic Acid	62
Linseed Oil	-4
Acetone	-94

Review

69.25

Fill in each (with >, <, or = to make a true statement. 4.NBT.2

46. 69.23 (

- 47. 171.10 (171.09
- 148. 47,74 47.740
- 49. Part of a sauce recipe is shown. If all the ingredients are mixed together, how much sauce will be made? 5.NF.1
- 50. Caroline's soccer practice starts at quarter after 4 P.M. and ends at 5 р.м. How many minutes does her soccer practice last? 4.MD.2

6 teaspoons Worcestershire Sauce 1½ teaspoons seasoned salt teaspoon onion powder 4 teaspoon garlic powder

Name:	

One-Step Equations Study Guide

One-step equations are solved using only one step! All you need to know are the following:

<u>Operations:</u> Addition, subtraction, multiplication and division can be seen in a one-step equation.

Inverse Operations: These are the opposite operations that undo the operation that is taking place in the one-step equation.

Operation	Inverse Operation		
Addition	Subtraction		
Subtraction	Addition		
Multiplication	Division		
Division	Multiplication		

Examples of the operation we will see...

Expression → Operation → Inverse Operation

$$x + 8 \rightarrow Addition \rightarrow Subtraction$$

$$x-8 \rightarrow Subtraction \rightarrow Addition$$

$$\frac{x}{4}$$
 \rightarrow Division \rightarrow Multiplication

$$3x \rightarrow Multiplication \rightarrow Division$$

One-step equations can be solved very easily if you ask yourself the following questions:

- 1. Read the equation out loud or in your head.
- 2. Determine the operation taking place.
- 3. Figure out what the inverse operation is.
- 4. Use the inverse operation to solve.
- 5. CHECK YOUR ANSWER!

Let's look at an example while using the 5 steps above...

2x = 10

- 1. "Two times a number equals ten." Here you should read the question out loud to figure out what is happening in the equation.
- 2. The operation taking place is multiplication. I know this because we see "2x" which means two times the variable.
- 3. Since our operation is multiplication our inverse operation is division.

	a		

- 4. Since we are multiplying by 2 in the equation we need to divide both sides by 2. This means we divide by 2 on both sides of the equal side. 2 divided by 2 gives us 1 so we are left with x. On the other side of the equal sign we have 10 divided by 2 which gives us 5. So, x = 5.
- 5. Now we need to check our answer to make sure we are right. If we plug 5 back in the equation, we see that we have 2(5) = 10 which gives us 10 = 10. So we know we were right!

Now it is time for you to practice...

1.
$$5x = 20$$

2.
$$7x = 28$$

3.
$$x + 9 = 18$$

4.
$$x + 2 = 7$$

5.
$$\frac{x}{4} = 10$$

6.
$$\frac{x}{3} = 12$$

7.
$$x - 7 = 14$$

8.
$$x - 8 = 12$$

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Notes Chapter 5: Lesson 1

Equations

An **equation** is a mathematical sentence showing two expressions are equal. An equation contains an **equal sign**, =. Some equations contain variables. When you replace a variable with a value that results in a true sentence, you **solve** the equation. The value for the variable is the solution of the equation.

Example 1

Solve 14 - p = 6 using guess, check, and revise.

Guess the value of p, then check it.

Try 7.

Try 6.

Try 8.

14 - p = 6

14 - p = 6

14 - p = 6

 $14 - 7 \neq 6$

 $14 - 6 \neq 6$

14 - 8 = 6

revise

revise

yes

The solution is 8 because replacing p with 8 results in a true sentence.

Example 2

Solve $15 \div m = 5$ mentally.

 $15 \div m = 5$

Think 15 divided by what number is 5?

 $15 \div 3 = 5$

You know that $15 \div 3 = 5$.

The solution is 3.

Exercises

Identify the solution of each equation from the list given (use your calculator).

1.
$$h + 19 = 56$$
; 36, 37, 38

2.
$$31 + x = 42$$
; 9, 10, 11

3.
$$k-4=13$$
; 16, 17, 18

4.
$$34 - b = 17$$
; 16, 17, 18

5.
$$5w = 30$$
; 5, 6, 7

6.
$$63 = 7k$$
, 7, 8, 9

7.
$$36 \div s = 9$$
; 4, 5, 6

7.
$$36 \div s = 9$$
; 4, 5, 6 8. $x \div 3 = 8$; 23, 24, 25

Solve each equation mentally.

9.
$$i + 3 = 9$$

9.
$$j + 3 = 9$$
 10. $14 + n = 19$

11.
$$23 + x = 29$$

12.
$$31 - h = 24$$
 13. $m - 5 = 11$

13.
$$m - 5 = 11$$

14.
$$3m = 27$$

15.
$$56 = 76$$

15.
$$56 = 7b$$
 16. $14 \div f = 2$

17.
$$j \div 8 = 4$$

15)
$$p - (9 - (m + q))$$
; use $m = 4$, $p = 5$, and $q = 3$ 16) $(a^2 - b) \div 6$; use $a = 5$, and $b = 1$

16)
$$(a^2 - b) \div 6$$
; use $a = 5$, and $b = 1$

17)
$$(6 + h^2 - j) \div 2$$
; use $h = 6$, and $j = 4$

18)
$$y - (4 - x - y \div 2)$$
; use $x = 3$, and $y = 2$

19)
$$x^3 \div 3 - y$$
; use $x = 3$, and $y = 1$

20)
$$(p+q)^2 - (5-5)$$
; use $p=1$, and $q=1$

21)
$$12k - h^2$$
; use $h = 2$, and $k = 3$

22)
$$y \div 5 + 1 + x \div 6$$
; use $x = 6$, and $y = 5$

23)
$$6 \div 6 + z + x - y$$
; use $x = 2$, $y = 5$, and $z = 6$

24)
$$y-z+xz \div 6$$
; use $x=3$, $y=4$, and $z=4$

25)
$$\frac{y}{2} + x + 4 + z + y$$
; use $x = 7$, $y = 2$, and $z = 4$ 26) $c \times \frac{bc}{4} - (7 - a)$; use $a = 4$, $b = 8$, and $c = 5$

26)
$$c \times \frac{bc}{4} - (7 - a)$$
; use $a = 4$, $b = 8$, and $c = 5$

4.		

Algebra Worksheet

Name _____ Date ____

$$\bigcirc$$
 7y - y = 30

$$4y + 4 - 9y = -46$$

$$9 + y6 = 78$$

$$9y + 9 = 72$$

Algebra Worksheet

ANSWER KEY

1)
$$7y - y = 30$$

 $y = 5$

$$3 5y + 2y + 10y = 51$$

$$y = 3$$

$$4y + 4 - 9y = -46$$

$$y = 10$$

$$y = 10$$
4y + 2y + 5y = 110

$$2y - 9 = -3$$

$$v = 3$$

$$9y + 9 = 72 y = 7$$

$$7y + 10 - 7y = 10$$

$$y = 7$$

Name

Date 12-9-19

Chapter 4 - Lesson 9: Equivalent Expressions/ Simplifying Expressions

Review

Commutative property: The order in which numbers are added or multiplied does not change the sum or the product

$$a+b=b+a$$
 or $a \cdot b = b \cdot a$

$$a \bullet b = b \bullet a$$

Associative property: The way in which numbers are grouped does not change the sum or the product

$$(a + b) + c = a (b + c)$$

$$(a+b)+c=a$$
 $(b+c)$ or $(a \cdot b) \cdot c=a \cdot (b \cdot c)$

• A ______ is each part of an expression that is separated by a plus or a minus. ex. 3x + 2y+4 3terms

When a term contains a number and a variable, the number is called the

coefficient. ex. 3x 3 is the coefficient

A term without a variable is called a <u>Constant</u> - doesn't change ex. ay - G• _____ contain the same variables. ex. 3x, 7, 7x, 10 x

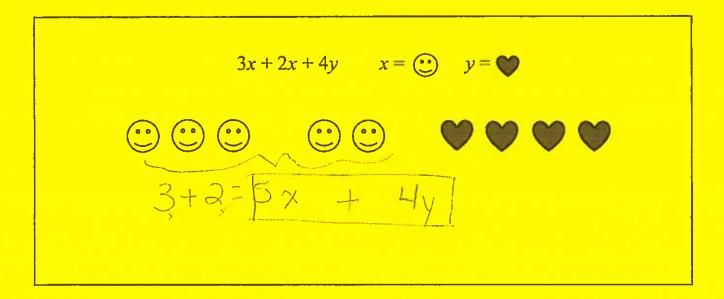
3x + 7 - x

Terms: 3x, 7, x 3 terms

Coefficient: 3

Constant: 7

Like terms: 3x and x



Example 1:

Simplify the expression 16 + (v + 4)

$$16 + (v + 4) = 16 + (4 + v)$$

$$= (16 + 4) + v$$

$$= 20 + v$$
commutative property
$$0 + (v + 4) = 16 + (4 + v)$$
associative property
$$0 + (v + 4) = 16 + (4 + v)$$
associative property

So, 16 + (v + 4) in simplified form is 20 + v

Example 2:

Simplify the expression 3x + (6y + 2x)

$$3x + (6y + 2x) = 3x + (2x + 6y)$$
 commutative property
$$= (3x + 2x) + 6y$$
 associative property
$$= 5x + 6y$$
 combine like terms

So, 3x + (6y + 2x) in simplified form is 5x + 6y

Practice problems

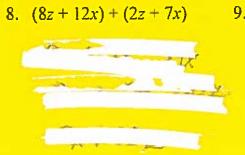
Simplify each expression. Justify each step.

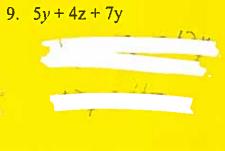
$$4. \ \underline{8x} + 5 + \underline{2x}$$

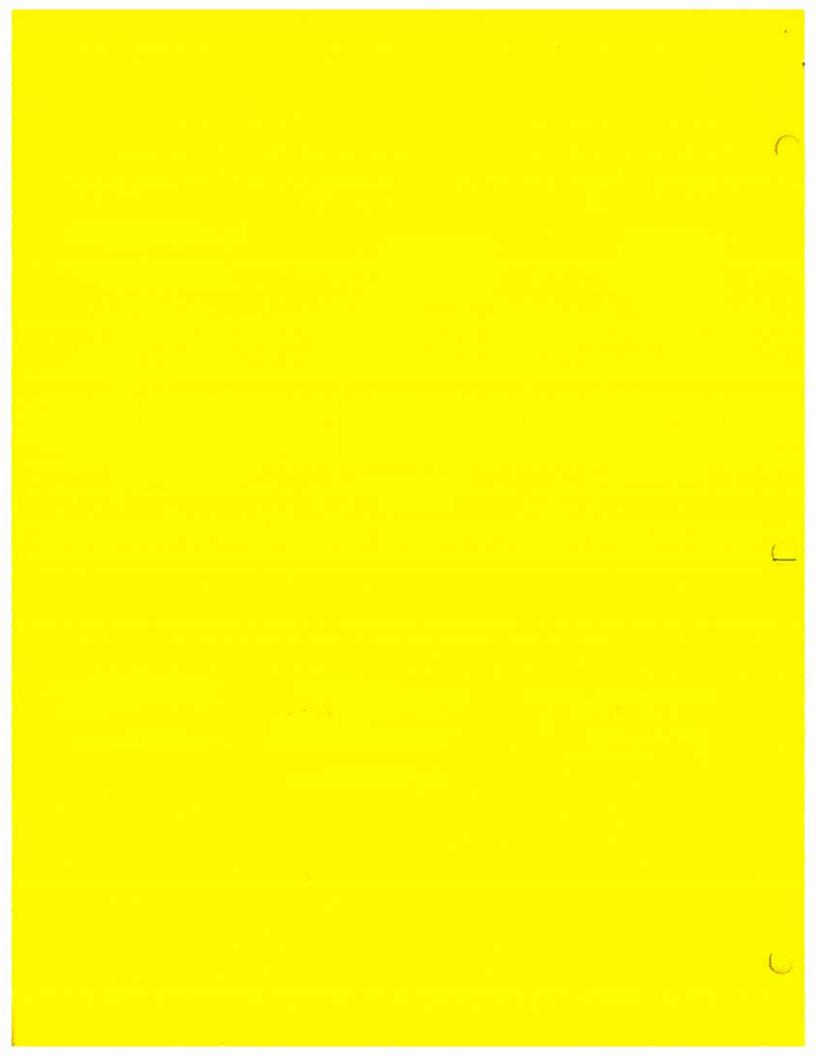
5.
$$(12 + 2u) + 3$$



7. 9x + (4z + 3x)





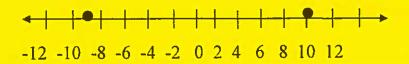


Quiz Review - Integers, Rational Numbers, Absolute Value, Coordinate Graphing

1) The coldest temperature James ever recorded at his house was 16 degrees below zero.

Which number represents this temperature?

- a) 16
- b) -16
- c) 0
- d) 1.6
- 2) What is the opposite of -8.
 - a) 8
 - b) 8.1
 - c) -8
 - d) 1/8
- 3) Which inequality is shown by the points on this number line?



- a) 10 > 9
- b) -9 < 10
- c) -9 > 10
- d) None of the above

4)	Dan ran 6,25 miles. Jo	te ran $6\frac{1}{2}$ miles.
	Who ran further? S a) Joe b) Dan	how your work to justify your answer.
5)	Sea Level is represente	ed by which integer?
	a) -1	
	b) 1	
	c) 0	
	d) None of the above	ve
6)	Seneca lost \$45.	
	Which is the correct int	teger?
	a) 0.45	
	b) 4.5	
	c) -45	
	d) 45	

7)	Which of the following is the opposite of the opposite of 5?				
	a) 0				
	b) 5				
	c) -5				
	d) 10				
0)					
8)	Evaluate. 12 + -6				
	a) 18				
	b) -18				
	c) 6				
	d) -6				
9)	Amy is building a house. The basement floor is at -13 feet. The roof of the house is above the ground at 25 feet. Write an inequality to compare the heights.				
10)	Order the set {-7, 5, 2, -9, 1, 0} from greatest to least.				

Write each fraction as a decimal. 11)

$$\frac{1}{2} =$$

$$\frac{1}{4} = \frac{3}{4} =$$

$$\frac{3}{4} =$$

Compare >, < or =. -16 \bigcirc -1512)

$$-0.86$$
 $-\frac{3}{4}$

13) Which statement is false?

a)
$$4 > -3$$

b)
$$1\frac{1}{5} > -1\frac{4}{5}$$

c)
$$\frac{3}{4} = -0.75$$

d)
$$1.5 > \frac{10}{9}$$

- The Grinch's homeroom raised \$1,259 for the local Elves' charity. Find the opposite of the opposite of this integer.
 a) -1,259
 b) 1,259
 - c) 9,521
 d) 1
- 15) The temperatures recorded for the week were as follows:
 -2, 32, -4, 13, -10, 14, 29
 List them in order from *coldest to warmest*.

- 16) To find the *Absolute Value* of a number means to see,
 - a) how far a number is from 100 on a number line
 - b) how far a number is from 0 on a number line
 - c) how far a number is from one on a number line
 - d) how far a number is from -1 on a number line
- 17) The absolute value of |-8| is _____
 - a) -8
 - b) $\frac{1}{8}$
 - c) 8.1
 - d) 8

18)	Fill in the • with <, >, or = to.
	-9.25 9.25
	a) >
	b) <
	c) =
19)	Megan was playing a game. She lost 10 points at the start of the game, but then she gained 22 points on her next turn. What is Megan's score?
	a) 32 points Answer:
	b) -22 points
	c) 4 points
	d) 12 points
20)	Which of the following does not mean "positive"?
	a) loss
	b) increase
	c) found
	d) gain
21)	Yesterday, the low temperature for was -1°F. Today, the temperature is 7°F. What is the difference between these two temperatures?
	a) 6°F
	b) -6°F Answer:
	c) 8°F
	d) -8°F

- 22) Is zero a) Negative, b) Positive, or c) Neither?
- 23) Which of the following is true about the opposite of 0?
 - a) Zero has no opposite.
 - b) Zero is its own opposite
 - c) Zero has a lot of opposites.
 - d) Zero is not a number, so it has no opposites.
- 24) Using the line below, create a number line from -12 to 12.



- a) Label -12 with the letter M.
- b) Label the opposite of M with a T.
- c) Label an integer between -10 and -8 with an A.
- d) Label the opposite of A with an N.
- e) Label the opposite of the opposite of -5 with the letter G.
- f) Label the integer -3 with the letter N
- g) Label the opposite of 0 with the letter I.
- h) Label the opposite of -1 with F
- i) Label the opposite of N (*from letter f*) with C.
- j) Label an integer between 5 and 9 with the letter E.
- k) Label the integer 2 with the letter I.
- 1) Complete this sentence with the word you created above:

		1 .
Math class is		1 1

25)	What is the coordinate point for the origin?
26)	What axis is horizontal?
27)	What axis is vertical?
28)	A coordinate plane is made up of 4 boxes that are called
29)	When locating coordinate points in one of the four, you use to tell which they are in.
30)	The point (-4,5) will be in which?
31)	Coordinate points that are in are both positive.
32)	To plot the coordinate point (5, -3), you would a) go left 5 spaces and up 3 spaces b) go right 5 spaces and up 3 spaces c) go right 5 spaces and down 3 spaces d) go left 5 spaces and down 3 spaces